

## Important Formulas

- Newtons Second Law  $F = ma$
- Formula of Weight  $w = mg$
- Relation Between Force and Momentum  $F = \frac{\Delta p}{\Delta t}$
- Centripetal Force  $F_c = \frac{mv^2}{r}$
- Frictional Force  $F_s = \mu mg$
- Relation Between Force and Momentum

$$F = \frac{\Delta p}{\Delta t}$$

- Impulse

$$\text{Impulse} = F \times \Delta t$$

$$\text{Impulse} = \frac{\Delta p}{\Delta t} \times \Delta t$$

$$\text{Impulse} = \Delta p$$

$$\text{Impulse} = \text{Change in momentum}$$

3.1. A 10 kg block is placed on a smooth horizontal surface. A horizontal force of 5 N is applied to the block. Find:

- (a) the acceleration produced in the block.
- (b) the velocity of block after 5 seconds.

## Given Data

$$\begin{aligned} \text{Mass of block} &= m = 10 \text{ kg} \\ \text{Force} &= F = 5 \text{ N} \\ \text{Initial velocity} &= v_i = 0 \text{ ms}^{-1} \end{aligned}$$

## To Find

$$\begin{aligned} \text{Acceleration} &= a = ? \\ \text{Final velocity} &= v_f = ? \end{aligned}$$

## Solution

According to second law of motion

$$\begin{aligned} F &= ma \\ 5 &= (10)(a) \\ \frac{5}{10} &= a \\ 0.5 &= a \\ a &= 0.5 \text{ ms}^{-2} \end{aligned}$$

Now by using first equation of motion

$$\begin{aligned} v_f &= v_i + at \\ v_f &= 0 + (0.5)(5) \\ v_f &= 0 + 2.5 \\ v_f &= 2.5 \text{ ms}^{-1} \end{aligned}$$

3.2. The mass of a person is 80 kg. What will be his weight on the Earth? What will be his weight on the Moon? The value of acceleration due to gravity of Moon is  $1.6 \text{ ms}^{-2}$ .

## Given Data

$$\begin{aligned} \text{Mass of body} &= m = 80 \text{ kg} \\ \text{Value of } g \text{ on the surface of Earth} &= g_E = 10 \text{ ms}^{-2} \\ \text{Value of } g \text{ on the surface of Moon} &= g_M = 1.6 \text{ ms}^{-2} \end{aligned}$$

## To Find

$$\begin{aligned} \text{Weight on the surface of Earth} &= w_E = ? \\ \text{Weight on the surface of Moon} &= w_M = ? \end{aligned}$$

## Solution

By using formula of weight  $w = mg$

$$\begin{aligned} w_E &= mg_E \\ w_E &= (80)(10) \\ w_E &= 800 \text{ N} \end{aligned}$$

Now again by using formula of weight  $w = mg$

$$\begin{aligned} w_M &= mg_M \\ w_M &= (80)(1.6) \\ w_M &= 128 \text{ N} \end{aligned}$$

3.3. What force is required to increase the velocity of 800 kg car from  $10 \text{ ms}^{-1}$  to  $30 \text{ ms}^{-1}$  in 10 seconds?

## Given Data

$$\begin{aligned} \text{Mass of car} &= m = 800 \text{ kg} \\ \text{Initial velocity} &= v_i = 10 \text{ ms}^{-1} \\ \text{Final velocity} &= v_f = 30 \text{ ms}^{-1} \\ \text{Time} &= t = 10 \text{ s} \end{aligned}$$

## To Find

$$\text{Force} = F = ?$$

## Solution

According to second law of motion

$$\begin{aligned} F &= ma \\ F &= (m) \left( \frac{v_f - v_i}{t} \right) \\ F &= (800) \left( \frac{30 - 10}{10} \right) \\ F &= (800) \left( \frac{20}{10} \right) \\ F &= (800)(2) \\ F &= 1600 \text{ N} \end{aligned}$$

3.4. A 5 g bullet is fired by a gun. The bullet moves with a velocity of  $300 \text{ ms}^{-1}$ . If the mass of the gun is 10 kg, find the recoil speed of the gun.

## Given Data

$$\text{Mass of bullet} = m = 5 \text{ g}$$

$$m = \frac{5}{1000} \text{ kg}$$

$$m = 0.005 \text{ kg}$$

$$\text{Velocity of bullet} = v = 300 \text{ ms}^{-1}$$

$$\text{Mass of gun} = M = 10 \text{ kg}$$

**To Find**

$$\text{Recoil speed of the gun} = V = ?$$

**Solution**

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before firing} &= \text{Total momentum after firing} \\ 0 &= MV + mv \\ 0 &= (10)V + (0.005)(300) \\ 0 &= 10V + 1.5 \\ -1.5 &= 10V \\ \frac{-1.5}{10} &= V \\ -0.15 &= V \\ V &= -0.15 \text{ ms}^{-1} \end{aligned}$$

Negative sign indicates the gun recoils. i.e. move in backward direction opposite to the motion of bullet.

**3.5. An astronaut weighs 70 kg. He throws a wrench of mass 300 g at a speed of 3.5 ms<sup>-1</sup>. Determine:**

- the speed of astronaut as he recoils away from the wrench.
- the distance covered by the astronaut in 30 minutes.

**Given Data**

$$\begin{aligned} \text{Mass of astronaut} &= M = 70 \text{ kg} \\ \text{Mass of wrench} &= m = 300 \text{ g} \\ m &= \frac{300}{1000} \text{ kg} \\ m &= 0.3 \text{ kg} \\ \text{Speed of wrench} &= v = 3.5 \text{ ms}^{-1} \\ \text{Time} &= t = 30 \text{ min.} \\ t &= 30 \times 60 \text{ s} \\ t &= 1800 \text{ s} \end{aligned}$$

**To Find**

$$\begin{aligned} \text{Recoil speed of the astronaut} &= V = ? \\ \text{Distance covered in 30 minutes} &= S = ? \end{aligned}$$

**Solution**

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before throwing} &= \text{Total momentum after throwing} \\ 0 &= MV + mv \\ 0 &= (70)V + (0.3)(3.5) \\ 0 &= 70V + 1.05 \\ -1.05 &= 70V \end{aligned}$$

$$\begin{aligned} \frac{-1.05}{70} &= V \\ -0.015 &= V \\ V &= -0.015 \text{ ms}^{-1} \\ V &= -1.5 \times 10^{-2} \text{ ms}^{-1} \end{aligned}$$

**Negative sign** indicates the astronaut recoils (moves in the opposite direction of the wrench).

Now by using formula of distance

$$\begin{aligned} S &= Vt \\ S &= (0.015)(1800) \\ S &= 27 \text{ m} \end{aligned}$$

We don't take negative speed for distance because: Distance is always positive. The negative sign shows direction, not how far something moves.

**3.6. A 6.5 × 10<sup>3</sup> kg bogie of a goods train is moving with a velocity of 0.8 ms<sup>-1</sup>. Another bogie of mass 9.2 × 10<sup>3</sup> kg coming from behind with a velocity of 1.2 ms<sup>-1</sup> collides with the first one and couples to it. Find the common velocity of the two bogies after they become coupled.**

**Given Data**

$$\begin{aligned} \text{Mass of first bogie} &= m_1 = 6.5 \times 10^3 \text{ kg} \\ \text{Velocity of first bogie} &= v_1 = 0.8 \text{ ms}^{-1} \\ \text{Mass of second bogie} &= m_2 = 9.2 \times 10^3 \text{ kg} \\ \text{Velocity of second bogie} &= v_2 = 1.2 \text{ ms}^{-1} \end{aligned}$$

**To Find**

$$\text{Common velocity after coupling} = V = ?$$

**Solution**

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before couple} &= \text{Total momentum after couple} \\ m_1v_1 + m_2v_2 &= m_1V + m_2V \\ m_1v_1 + m_2v_2 &= V(m_1 + m_2) \\ (6.5 \times 10^3)(0.8) + (9.2 \times 10^3)(1.2) &= V[(6.5 \times 10^3) + (9.2 \times 10^3)] \\ 5200 + 11040 &= V(15700) \\ \frac{16240}{15700} &= V \\ 1.03 &= V \\ V &= 1.03 \text{ ms}^{-1} \end{aligned}$$

**3.7. A cyclist weighing 55 kg rides a bicycle of mass 5 kg. He starts from rest and applies a force of 90 N for 8 seconds. Then he continues at a constant speed for another 8 seconds. Calculate the total distance travelled by the cyclist.**

**Given Data**

$$\begin{aligned} \text{Mass of cyclist} &= m_1 = 55 \text{ kg} \\ \text{Mass of bicycle} &= m_2 = 5 \text{ kg} \\ \text{Total mass} &= m = 55 \text{ kg} + 5 \text{ kg} \\ m &= 60 \text{ kg} \end{aligned}$$

$$\begin{aligned}\text{Force applied} &= F = 90 \text{ N} \\ \text{Time of acceleration} &= t_1 = 8 \text{ s} \\ \text{Time of constant speed} &= t_2 = 8 \text{ s} \\ \text{Initial speed} &= v_i = 0 \text{ ms}^{-1}\end{aligned}$$

**To Find**

$$\text{Total distance travelled} = S = ?$$

**Solution**

According to second law of motion

$$\begin{aligned}F &= ma \\ 90 &= (60)(a) \\ \frac{90}{60} &= a \\ 1.5 &= a \\ a &= 1.5 \text{ ms}^{-2}\end{aligned}$$

Now by using first equation of motion

$$\begin{aligned}v_f &= v_i + at_1 \\ v_f &= 0 + (1.5)(8) \\ v_f &= 0 + 12 \\ v_f &= 12 \text{ ms}^{-1}\end{aligned}$$

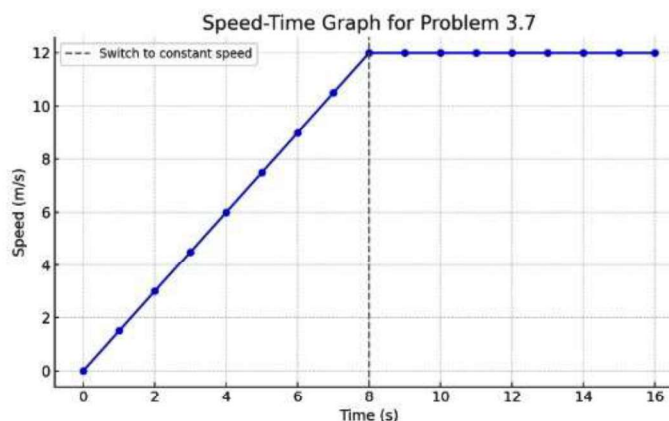
Distance covered **during acceleration** by using second equation of motion

$$\begin{aligned}S_1 &= v_i t_1 + \frac{1}{2} a t_1^2 \\ S_1 &= (0)(8) + \frac{1}{2} (1.5)(8)^2 \\ S_1 &= 0 + \frac{1}{2} (1.5)(64) \\ S_1 &= 0 + 48 \\ S_1 &= 48 \text{ m}\end{aligned}$$

Distance covered at **constant speed** by formula  $S = vt$

$$\begin{aligned}S_2 &= v_f t_2 \\ S_2 &= (12)(8) \\ S_2 &= 96 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Total distance travelled} &= S = S_1 + S_2 \\ S &= 48 \text{ m} + 96 \text{ m} \\ S &= 144 \text{ m}\end{aligned}$$



**3.8. A ball of mass 0.4 kg is dropped on the floor from a height of 1.8 m. The ball rebounds straight upward to a height of 0.8 m. What is the magnitude and direction of the impulse applied to the ball by the floor?**

**Given Data**

$$\begin{aligned}\text{Mass of ball} &= m = 0.4 \text{ kg} \\ \text{Drop height} &= h_1 = 1.8 \text{ m} \\ \text{Rebound height} &= h_2 = 0.8 \text{ m} \\ \text{Acceleration due to gravity} &= g = 10 \text{ ms}^{-2}\end{aligned}$$

**To Find**

$$\text{Impulse (magnitude and direction)} = ?$$

**Solution**

Since the ball is dropped so,  $v_i = 0 \text{ ms}^{-1}$

$$\begin{aligned}2gh_1 &= v_f^2 - v_i^2 \\ 2(10)(1.8) &= v_f^2 - (0)^2 \\ 36 &= v_f^2 \\ v_f^2 &= 36 \\ \sqrt{v_f^2} &= \sqrt{36} \\ v_f &= \pm 6 \text{ ms}^{-1}\end{aligned}$$

But since the ball is moving downward, we select the negative root. i. e

$$v_f = v_{\text{before}} = -6 \text{ ms}^{-1}$$

At maximum rebound height,  $v_f = 0 \text{ ms}^{-1}$

$$\begin{aligned}2gh_2 &= v_f^2 - v_i^2 \\ 2(-10)(0.8) &= (0)^2 - v_i^2 \quad (\because \text{ball moving upward}) \\ -16 &= -v_i^2 \\ v_i^2 &= 16 \\ \sqrt{v_i^2} &= \sqrt{16} \\ v_i &= \pm 4 \text{ ms}^{-1}\end{aligned}$$

But since the ball is moving upward, we select the positive root. i. e

$$v_i = v_{\text{after}} = 4 \text{ ms}^{-1}$$

Now by using formula of impulse

$$\begin{aligned}\text{Impulse} &= \text{Change in momentum} \\ &= \Delta p \\ &= p_f - p_i \\ &= mv_f - mv_i \\ &= m(v_f - v_i) \\ &= m(v_{\text{after}} - v_{\text{before}}) \\ &= (0.4)[4 - (-6)] \\ &= (0.4)[10]\end{aligned}$$

$$\text{Impulse} = 4 \text{ Ns}$$

The **positive result** means the impulse is **upward** (floor pushes the ball up).

**Note:** In physics, we always choose a reference direction to be positive.

For vertical motion:

- We choose upward as positive (by convention).
- So, any velocity in the upward direction is positive.
- And any velocity in the downward direction is negative.

**3.9. Two balls of masses 0.2 kg and 0.4 kg are moving towards each other with velocities  $20 \text{ ms}^{-1}$  and  $5 \text{ ms}^{-1}$  respectively. After collision, the velocity of 0.2 kg ball becomes  $6 \text{ ms}^{-1}$ . What will be the velocity of 0.4 kg ball?**

**Given Data**

Mass of ball A =  $m_1 = 0.2 \text{ kg}$

Mass of ball B =  $m_2 = 0.4 \text{ kg}$

Initial velocity of ball A =  $v_1 = 20 \text{ ms}^{-1}$

Initial velocity of ball B =  $v_2 = -5 \text{ ms}^{-1}$  (opposite direction)

Final velocity of ball A =  $v'_1 = 6 \text{ ms}^{-1}$

**To Find**

Final velocity of ball B =  $v'_2 = ?$

**Solution**

According to law of conservation of momentum

total momentum of the system before collision = total momentum of the system after collision

$$m_1 v_1 + m_2 v_2 = m_1 v'_1 + m_2 v'_2$$

$$(0.2)(20) + (0.4)(-5) = (0.2)(6) + (0.4)(v'_2)$$

$$4 - 2 = 1.2 + (0.4)(v'_2)$$

$$2 - 1.2 = 0.4 v'_2$$

$$0.8 = 0.4 v'_2$$

$$\frac{0.8}{0.4} = v'_2$$

$$2 = v'_2$$

$$v'_2 = 2 \text{ ms}^{-1}$$