Power = P = ?

Important Formulas

$$ightharpoonup Work Done W = FS \implies W = FS \cos \theta$$

$$Fine Energy E_k = \frac{1}{2} m v^2$$

$$ightharpoonup$$
 Potential Energy $E_p = mgh$

$$\blacktriangleright$$
 Mass Energy Equation $E = mc^2$

Power
$$power = \frac{work}{time} \Rightarrow P = \frac{W}{t}$$

Mass Energy Equation
$$E = mc$$

Power $power = \frac{work}{time} \Rightarrow P = \frac{W}{t}$

Efficiency $Efficiency = \frac{output}{input}$

$$\% \ Efficiency = \frac{output}{input} \times 100$$

$$\triangleright$$
 Weight $w = mg$

5.1. A force of 20 N acting at an angle of 60° to the horizontal is used to pull a box through a distance of 3 macross a floor. How much work is done? **Given Data**

$$Force = F = 20 N$$

 $Angle = \theta = 60^{\circ}$
 $Distance\ covered = S = 3 m$

To Find

$$Work\ done = W = ?$$

Solution

By using formula of work done

$$W = FS \cos \theta$$

 $W = (20)(3) \cos 60^{\circ}$
 $W = (20)(3)(0.5)$
 $W = 30 I$

5.2. A body moves a distance of 5 metres in a straight line under the action of a force of 8 newtons. If the work done is 20 Joules, find the angle which the force makes with the direction of motion of the body. Given Data

Distance covered =
$$S = 5 m$$

Force = $F = 8 N$
Work done = $W = 20 I$

To Find

$$Angle = \theta = 3$$

Solution

By using formula of work

$$w = FS \cos \theta$$

$$w = FS \cos \theta$$

$$\cos \theta = \frac{W}{FS}$$

$$\cos \theta = \frac{20}{(8)(5)}$$

$$\cos \theta = \frac{20}{40}$$

$$\cos \theta = 0.5$$

$$\theta = \cos^{-1}(0.5)$$

$$\theta = 60^{\circ}$$

5.3. An engine raises 100 kg of water through a height of 80 m in 25 s. What is the power of the engine? **Given Data**

Mass of water =
$$m = 100 kg$$

Height raised = $h = 80 m$
Time taken = $t = 25 s$

To Find

Power =
$$\frac{Work}{time}$$

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{mgh}{t} \quad \because F = W = mg \& S = h$$

$$P = \frac{(100)(10)(80)}{25}$$

$$P = 3200 W$$

5.4. A body of mass 20 kg is at rest. A 40 on it for 5 seconds. What is the kinetic energy of the body at the end of this time? Given Data

Mass of body =
$$n = 20 \text{ kg}$$

Initial velocity = $v_i = 0 \text{ ms}^{-1}$
Korce = $F = 40 \text{ N}$

To Find

Kinetic energy =
$$E_k = ?$$

and law of motion

$$F = ma$$

$$40 = (20)(a)$$

$$\frac{40}{20} = a$$

$$2 = a$$

$$a = 2 ms^{-2}$$

For final velocity using first equation of motion

$$v_f = v_i + gt$$

 $v_f = 0 + (2)(5)$
 $v_f = 10 \text{ ms}^{-1}$
 $v = 10 \text{ ms}^{-1}$

Now, by using formula of kinetic energy

$$E_k = \frac{1}{2}mv^2$$

$$E_k = \frac{1}{2}(20)(10)^2$$

$$E_k = \frac{1}{2}(20)(100)$$

$$E_k = 1000 J$$

5.5. A ball of mass 160 g is thrown vertically upward. The ball reaches a height of 20 m. Find the potential energy gained by the ball at this height.

Given Data

Mass of ball =
$$m = 160 g$$

$$m = \frac{160}{1000} kg$$

$$m = 0.16 kg$$

$$Height\ reached = h = 20\ m$$

Gravitational acceleration = $g = 10 \text{ ms}^{-2}$ To Find

Potential energy = E_p = ?

Solution

By using formula of potential energy

$$E_p = mgh$$

 $E_p = (0.16)(10)(20)$
 $E_n = 32 J$

5.6. A 0.14 kg ball is thrown vertically upward with an initial velocity of $35 ms^{-1}$. Find the maximum height reached by the ball.

Given Data

Mass of ball =
$$m = 0.14 kg$$

Initial velocity = $v = 35 ms^{-1}$

Gravitational acceleration = $g = 10 \text{ ms}^{-2}$

To Find

 $Maximum\ height\ reached=h=?$

Solution

At the maximum height, all the kinetic energy of the ball is converted into potential energy.

$$E_p = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$h = \frac{mv^2}{2mg}$$

$$h = \frac{v^2}{2g}$$

$$h = \frac{(35)^2}{2(10)}$$

$$h = \frac{1225}{20}$$

$$h = 61.25 m$$

5.7. A girl is swinging on a swing. At the lowest points her swing, she is 1.2 m from the ground, and at the highest point she is $2.0\,m$ from the ground. What is her maximum velocity and where?

Given Data

Height at lowest point =
$$h_1 = 1.2 m$$

Height at highest point = $h_2 = 2.0 m$
Change in height = $h = h_2 - h_1$
 $h = 2.0 - 1.2$
 $h = 0.8 m$

Gravitational a celeration = $g = 10 \text{ ms}^{-2}$

To Find

lowest point, all the potential energy is ated into kinetic energy. So,

$$E_p = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$\frac{2mgh}{m} = v^2$$

$$2gh = v^2$$

$$v^2 = 2gh$$

$$\sqrt{v^2} = \sqrt{2gh}$$

$$v = \sqrt{(2)(10)(0.8)}$$

$$v = \sqrt{16}$$

$$v = 4 ms^{-1}$$

The $maximum\ velocity$ is $4\ ms^{-1}$, and it occurs at the lowest point of the swing.

5.8. A person pushes a lawn mower with a force of 50 N making an angle of 45° with the horizontal. If the mower is moved through a distance of 20 m, how much work is done?

Given Data

Force =
$$F = 50 N$$

Angle = $\theta = 45^{\circ}$
Distance = $S = 20 m$
Work done = $W = ?$
of work done
 $W = FS \cos \theta$

To Find

$$Work\ done = W = ?$$

Solution

By using formula of work done

$$W = FS \cos \theta$$

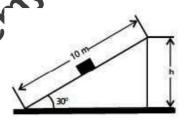
$$W = (50)(20) \cos 45$$

$$W = (50)(20)(070)$$

$$W = 707 J$$

5.9. Calculate the work done in

(i) Pushing a 5 kg inclined plane 10 m long that makes an angle of 30° with the horizontal.



il) Lifting the box vertically up from the ground to the top of the inclined plane.

Given Data

$$Mass\ of\ box = m = 5\ kg$$

$$Length\ of\ inclined\ plane = S = 10\ m$$

$$Angle\ with\ horizontal = \theta = 30^{\circ}$$

$$Gravitational\ acceleration = g = 10\ ms^{-2}$$

To Find

Work done along the incline
$$= W = ?$$

Work done in lifting the box vertically $= W = ?$
Dution (i)

The force needed to push the box up the slope is the component of weight along the incline:

$$F = mg \sin \theta$$

Using the formula for work

$$W = FS$$

$$W = (mg \sin \theta)(S)$$

$$W = (5)(10)(\sin 30^{\circ})(10)$$

$$W = (5)(10)(0.5)(10)$$

$$W = 250 I$$

(ii) Given figure forms a right-angle triangle so for height use trigonometric ratio

$$\sin \theta = \frac{Perpendicular}{Hypotenuse}$$

$$\sin 30^{\circ} = \frac{h}{10}$$

$$(10)(\sin 30^{\circ}) = h$$

$$(10)(0.5) = h$$

$$5 = h$$

$$h = 5 m$$

The work done against gravity is equal to the change in potential energy:

$$W = E_p$$

 $W = mgh$
 $W = (5)(10)(5)$
 $W = 250 J$

5.10. A box of mass 10~kg is pushed up along a ramp 15 m long with a force of 80 N. If the box rises up a height of 5 m, what is the efficiency of the system? **Given Data**

Mass of box =
$$m = 10 \text{ kg}$$

Length of ramp = $S = 15 \text{ m}$
Force applied = $F = 80 \text{ N}$
Height raised = $h = 5 \text{ m}$

Gravitational acceleration = $g = 10 \text{ ms}^{-2}$

To Find

$$Efficiency of the system = ?$$

Solution

The total energy supplied is the work done (input). By using formula of work done

$$W_{input} = FS$$

$$W_{input} = (80)(15)$$

$$W_{input} = 1200 J$$

The useful energy is the work done (output) to lift the box to height h.

$$W_{output} = mgh$$

 $W_{output} = (10)(10)(5)$
 $W_{output} = 500 J$

By using formula of efficiency

% Efficiency =
$$\frac{W_{output}}{W_{input}} \times 100$$

% Efficiency = $\frac{500}{1200} \times 100$
% Efficiency = $\frac{50000}{1200}$
% Efficiency = 41.720

5.11. A force of 600 N acts on a box to push it 5 m in 15 s. Calculate the power

Given Data

Force =
$$F = 600 N$$

Distance = $S = 5 m$
 $Time = t = 15 s$

$$Power = P = 3$$

Solution

g formula of power

Power =
$$\frac{W \text{ or } k}{\text{time}}$$

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{(600)(5)}{15}$$

$$P = 200 \text{ wat}$$

5.12. A 40 kg boy runs up-stair 10 m high in 8 s. What power he developed.

Given Data

Mass of boy =
$$m = 40 kg$$

Height = $h = 10 m$
Time = $t = 8 s$

To Find

$$Power = P = ?$$

Solution

By using formula of power

Power =
$$\frac{Work}{time}$$

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{mgh}{t} \quad \because F = W = mg \& S = h$$

$$P = \frac{(40)(10)(10)}{5}$$

$$P = 500 W$$

5.13. A force F acts through a distance L on a body. The force is then increased to 2F that further acts through 2L. Sketch a force-displacement graph and calculate the total work done.

Given Dat

Force for distance
$$L = F$$

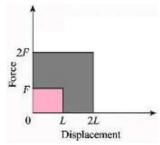
Force for distance $2L = 2F$

$$Work\ done = W = ?$$

Solution

As, the area under a forcedistance graph represents the work done by the force

 $Work\ done = 5\ unit$



Work done = Area under the graph
=
$$(F \times L) + (2F \times 2L)$$

= $FL + 4FL$
= $\mathbf{5FL}$

P = 200 watt