

Numerical Problems

## Important formulas

- Quantization Rule  $Q = ne$
- Energy supplied by the charge  $E = q(V_a - V_b)$
- Coulomb's Law  $F = k \frac{q_1 q_2}{r^2}$ ,  $k = 9 \times 10^9 \text{ Nm}^2 \text{C}^{-2}$
- Electric Field Intensity  $E = \frac{F}{q_0}$
- Electric Potential  $V = \frac{W}{q}$
- Capacitor and Capacitance Formula  $Q = CV$
- Equivalent Capacitance For Series Combination  
 $\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$
- Equivalent Capacitance For Parallel Combination  
 $C_{eq} = C_1 + C_2$

**13.1** The charge of how many negatively charged particles would be equal to  $100 \mu\text{C}$ . Assume charge on one negative particle is  $1.6 \times 10^{-19} \text{C}$ ? (ALP)

## Given Data

$$\text{Charge} = Q = 100 \mu\text{C}$$

$$Q = 100 \times 10^{-6} \text{C}$$

$$\text{Charge on electron} = e = 1.6 \times 10^{-19} \text{C}$$

## To Find

$$\text{No. of charged particles} = n = ?$$

## Solution

By using quantization rule

$$Q = ne$$

$$n = \frac{Q}{e}$$

$$n = \frac{100 \times 10^{-6} \text{C}}{1.6 \times 10^{-19} \text{C}}$$

$$n = 6.25 \times 10^{14}$$

**13.2** Two point charges  $q_1 = 10 \mu\text{C}$  and  $q_2 = 5 \mu\text{C}$  are placed at distance of  $150 \text{ cm}$ . What will be the Coulomb's force between them? Also find the direction of the force. (ALP)

## Given Data

$$q_1 = 10 \mu\text{C}$$

$$q_1 = 10 \times 10^{-6} \text{C}$$

$$q_2 = 5 \mu\text{C}$$

$$q_2 = 5 \times 10^{-6} \text{C}$$

$$r = 150 \text{ cm}$$

$$r = 150 \times 10^{-2} \text{m}$$

$$r = 1.5 \text{ m}$$

## To Find

$$\text{Coulomb's force} = F = ?$$

$$\text{Direction of force} = ?$$

## Solution

By using formula of coulomb's law

$$F = k \frac{q_1 q_2}{r^2}$$

$$F = (9 \times 10^9) \frac{(10 \times 10^{-6})(5 \times 10^{-6})}{(1.5)^2}$$

$$F = \frac{0.45}{2.25}$$

$$F = 0.2 \text{ N}$$

**Direction:** As both charges are same so force between two charges is repulsive (force of repulsion)

**13.3** The force of repulsion between two identical positive charges is  $0.8 \text{ N}$ , when the charges are  $0.1 \text{ m}$  apart. Find the value of each charge. (ALP)

## Given Data

As both charges are identical, so

$$q_1 = q_2 = q$$

$$\text{Force} = F = 0.8 \text{ N}$$

$$\text{Distance} = r = 0.1 \text{ m}$$

## To Find

$$\text{Value of each charge} = q = ?$$

## Solution

By using formula of coulomb's law

$$F = k \frac{q_1 q_2}{r^2}$$

$$F = k \frac{(q)(q)}{r^2}$$

$$F = \frac{kq^2}{r^2}$$

$$q^2 = \frac{Fr^2}{k}$$

$$q^2 = \frac{(0.8)(0.1)^2}{9 \times 10^9}$$

$$q^2 = 8.89 \times 10^{-13}$$

$$\sqrt{q^2} = \sqrt{8.89 \times 10^{-13}}$$

$$q = 9.42 \times 10^{-7} \text{ C}$$

**13.4** Two charges repel each other with a force of  $0.1 \text{ N}$  when they are  $5 \text{ cm}$  apart. Find the forces between the same charges when they are  $2 \text{ cm}$  apart. (ALP)

## Given Data

As both charges repel each other, they are similar charges, so

$$q_1 = q_2 = q$$

$$F_1 = 0.1 \text{ N}$$

$$r_1 = 5 \text{ cm}$$

$$r_1 = \frac{5}{100} \text{ m}$$

$$r_1 = 0.05 \text{ m}$$

## To Find

$$F_2 = ? \text{ when } r_2 = 2 \text{ cm} = 0.02 \text{ m}$$

## Solution

By using formula of coulomb's law

$$F_1 = k \frac{q_1 q_2}{r_1^2}$$

$$F_1 = k \frac{(q)(q)}{r_1^2}$$

$$F_1 = \frac{kq^2}{r_1^2}$$

$$q^2 = \frac{F_1 r_1^2}{k}$$

$$q^2 = \frac{(0.1)(0.05)^2}{9 \times 10^9}$$

$$q^2 = 2.78 \times 10^{-14}$$

$$\sqrt{q^2} = \sqrt{2.78 \times 10^{-14}}$$

$$q = 1.67 \times 10^{-7} \text{ C}$$

Now for  $F_2$

$$F_2 = k \frac{q_1 q_2}{r_2^2}$$

$$F_2 = k \frac{(q)(q)}{r_2^2}$$

$$F_2 = \frac{kq^2}{r_2^2}$$

$$F_2 = \frac{(9 \times 10^9)(1.67 \times 10^{-7})^2}{(0.02)^2}$$

$$F_2 = 6.22 \times 10^{-1} N$$

$$F_2 = 0.62 N$$

**13.5** The electric potential at a point in an electric field is  $10^4 V$ . If a charge of  $+100 \mu C$  is brought from infinity to this point. What would be the amount of work done on it? (ALP)

**Given Data**

$$\text{Electric potential} = V = 10^4 V$$

$$\text{Charge} = q = 100 \mu C$$

$$q = 100 \times 10^{-6} C$$

**To Find**

$$\text{Work done} = W = ?$$

**Solution**

By using formula of electric potential

$$V = \frac{W}{q}$$

$$W = qV$$

$$W = (100 \times 10^{-6})(10^4)$$

$$W = 1 J$$

**13.6** A point charge of  $+2 C$  is transferred from a point at potential  $100 V$  to a point at potential  $50 V$ , what would be the energy supplied by the charge? (ALP)

**Given Data**

$$\text{Charge} = Q = 2 C$$

$$\text{Higher potential} = V_a = 100 V$$

$$\text{Lower potential} = V_b = 50 V$$

**To Find**

$$\text{Energy supplied by charge} = E = ?$$

**Solution**

By using formula of energy supplied

$$E = q(V_a - V_b)$$

$$E = 2(100 - 50)$$

$$E = 2(50)$$

$$E = 100 J$$

**13.7** A capacitor holds  $0.06 \text{ coulombs}$  of charge when fully charged by a  $9 \text{ volt}$  battery. Calculate capacitance of the capacitor. (ALP)

**Given Data**

$$\text{Charge} = Q = 0.06 C$$

$$\text{Voltage} = V = 9 V$$

**To Find**

$$\text{Capacitance of capacitor} = C = ?$$

**Solution**

By using formula of capacitance

$$Q = CV$$

$$C = \frac{Q}{V}$$

$$C = \frac{0.06}{9}$$

$$C = 6.67 \times 10^{-3} F$$

**13.8** A capacitor holds  $0.03 \text{ coulombs}$  of charge when fully charged by a  $6 \text{ volt}$  battery. How much voltage would be required for it to hold  $2 \text{ coulombs}$  of charge? (ALP)

**Given Data**

$$Q_1 = 0.03 C$$

$$V_1 = 6 V$$

$$Q_2 = 2 C$$

**To Find**

$$V_2 = ?$$

**Solution**

By using formula of capacitance

$$Q = CV$$

$$C = \frac{Q}{V}$$

Capacitance for 1<sup>st</sup> capacitor

$$C = \frac{Q_1}{V_1} \dots (i)$$

Capacitance for 2<sup>nd</sup> capacitor

$$C = \frac{Q_2}{V_2} \dots (ii)$$

Comparing equation (i) and (ii)

$$\frac{Q_1}{V_1} = \frac{Q_2}{V_2}$$

$$Q_1 V_2 = Q_2 V_1$$

$$V_2 = \frac{Q_2 V_1}{Q_1}$$

$$V_2 = \frac{(2)(6)}{0.03}$$

$$V_2 = 400 V$$

**13.9.** Two capacitors of capacitance  $6 \mu F$  and  $12 \mu F$  are connected in series with a  $12V$  battery. Find the equivalent capacitance of the combination. Find the charge and their potential difference across each capacitor. (ALP)

**Given Data**

$$C_1 = 6 \mu F$$

$$C_2 = 12 \mu F$$

$$V = 12 V$$

**To Find**

$$C_{eq} = ?$$

$$Q_1 = ?, \quad Q_2 = ?$$

$$V_1 = ?, \quad V_2 = ?$$

**Solution**

By using formula of equivalent capacitance for series combination

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\frac{1}{C_{eq}} = \frac{1}{6 \mu F} + \frac{1}{12 \mu F}$$

$$\frac{1}{C_{eq}} = \frac{2 + 1}{12 \mu F}$$

$$\frac{1}{C_{eq}} = \frac{3}{12 \mu F}$$

$$\frac{1}{C_{eq}} = \frac{1}{4 \mu F}$$

$$C_{eq} = 4 \mu F$$

Charge will be same for each capacitor in series combination, so  $Q = Q_1 = Q_2$

$$Q = C_{eq}V$$

$$= (4 \mu F)(12 V)$$

$$Q = 48 \mu C$$

Voltage across 1<sup>st</sup> capacitor

$$Q = C_1 V_1$$

$$V_1 = \frac{Q}{C_1}$$

$$V_1 = \frac{48 \mu C}{6 \mu F}$$

$$V_1 = 8 V$$

Voltage across 2<sup>nd</sup> capacitor

$$Q = C_2 V_2$$

$$V_2 = \frac{Q}{C_2}$$

$$V_2 = \frac{48 \mu C}{12 \mu F}$$

$$V_2 = 4 V$$

**13.10. Two capacitors of capacitances of  $6 \mu F$  and  $12 \mu F$  are connected in parallel with a  $12 V$  battery. Find the equivalent capacitance of the combination. Find the charge and the potential difference across each capacitor. (ALP)**

**Given Data**

$$C_1 = 6 \mu F$$

$$C_2 = 12 \mu F$$

$$V = 12 V$$

**To Find**

$$C_{eq} = ?$$

$$Q_1 = ?, \quad Q_2 = ?$$

$$V_1 = ?, \quad V_2 = ?$$

**Solution**

By using formula of equivalent capacitance for parallel combination

$$C_{eq} = C_1 + C_2$$

$$C_{eq} = 6 \mu F + 12 \mu F$$

$$C_{eq} = 18 \mu F$$

As potential difference (voltage) will be same for each capacitor in parallel combination, so

$$V = V_1 = V_2 = 12 V$$

Charge across 1<sup>st</sup> capacitor

$$Q_1 = C_1 V_1$$

$$Q_1 = (6 \mu F)(12 V)$$

$$Q_1 = 72 \mu C$$

Charge across 2<sup>nd</sup> capacitor

$$Q_2 = C_2 V_2$$

$$Q_2 = (12 \mu F)(12 V)$$

$$Q_2 = 144 \mu C$$

### Examples

**13.1 Two bodies are oppositely charged with  $500 \mu C$  and  $100 \mu C$  charge. Find the force between the two charges if the distance between them in air is  $0.5 m$ . (ALP)**

**Given Data**

$$q_1 = 500 \mu C$$

$$q_1 = 500 \times 10^{-6} C$$

$$q_2 = 100 \mu C$$

$$q_2 = 100 \times 10^{-6} C$$

$$r = 0.5 m$$

**To Find**

$$Force = F = ?$$

**Solution**

By using formula of coulomb's law

$$F = k \frac{q_1 q_2}{r^2}$$

$$F = (9 \times 10^9) \frac{(500 \times 10^{-6})(100 \times 10^{-6})}{(0.5)^2}$$

$$F = \frac{450}{0.25}$$

$$F = 1800 N$$

**13.2 The capacitance of a parallel plate capacitor is  $100 \mu F$ . If the potential difference between its plates is  $50 volts$ , find the quantity of charge stored on each plate. (ALP)**

**Given Data**

$$Capacitance = C = 100 \mu F$$

$$C = 100 \times 10^{-6} F$$

$$Voltage = V = 50 V$$

**To Find**

$$Charge = Q = ?$$

**Solution**

By using formula of capacitance

$$Q = CV$$

$$Q = (100 \times 10^{-6})(50)$$

$$Q = 5 \times 10^{-3} C$$

$$Q = 5 mC$$

**13.3 Three capacitors with capacitances of  $3.0 \mu F$ ,  $4.0 \mu F$ , and  $5.0 \mu F$  are arranged in parallel combination with a battery of  $6 V$ , where  $1 \mu F = 10^{-6} F$ . Find (a) the total capacitance (b) the voltage across each capacitor (c) the quantity of charge on each plate of the capacitor. (ALP)**

**Given Data**

$$C_1 = 3.0 \mu F$$

$$C_2 = 4.0 \mu F$$

$$C_3 = 5.0 \mu F$$

$$V = 6 V$$

**To Find**

$$C_{eq} = ?$$

$$V_1 = ?, V_2 = ?, V_3 = ?$$

$$Q_1 = ?, Q_2 = ?, Q_3 = ?$$

**Solution**

By using formula of equivalent capacitance for parallel combination

$$C_{eq} = C_1 + C_2 + C_3$$

$$C_{eq} = 3.0 \mu F + 4.0 \mu F + 5.0 \mu F$$

$$C_{eq} = 12 \mu F$$

As potential difference (voltage) will be same for each capacitor in parallel combination, so

$$V = V_1 = V_2 = V_3 = 6 V$$

Charge across 1<sup>st</sup> capacitor

$$Q_1 = C_1 V_1$$

$$Q_1 = (3.0 \mu F)(6 V)$$

$$Q_1 = 18 \mu C$$

Charge across 2<sup>nd</sup> capacitor

$$Q_2 = C_2 V_2$$

$$Q_2 = (4.0 \mu F)(6 V)$$

$$Q_2 = 24 \mu C$$

Charge across 3<sup>rd</sup> capacitor

$$Q_2 = C_2 V_2$$

$$Q_2 = (5.0 \mu F)(6 V)$$

$$Q_2 = 30 \mu C$$

**13.4 Three capacitors with capacitances of  $3.0 \mu F$ ,  $4.0 \mu F$ , and  $5.0 \mu F$  are arranged in series combination to a battery of  $6 V$ , where  $1 \mu F = 10^{-6} F$ . Find (a) the total capacitance of the series combination. (b) the quantity of charge across each capacitor. (c) the voltage across each capacitor. (ALP)**

**Given Data**

$$C_1 = 3.0 \mu F$$

$$C_2 = 4.0 \mu F$$

$$C_3 = 5.0 \mu F$$

$$V = 6 V$$

**To Find**

$$C_{eq} = ?$$

$$V_1 = ?, V_2 = ?, V_3 = ?$$

$$Q_1 = ?, Q_2 = ?, Q_3 = ?$$

**Solution**

By using formula of equivalent capacitance for series combination

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

$$\frac{1}{C_{eq}} = \frac{1}{3.0 \mu F} + \frac{1}{4.0 \mu F} + \frac{1}{5.0 \mu F}$$

$$\frac{1}{C_{eq}} = \frac{20 + 15 + 12}{60 \mu F}$$

$$\frac{1}{C_{eq}} = \frac{47}{60 \mu F}$$

$$C_{eq} = \frac{60 \mu F}{47}$$

$$C_{eq} = 1.3 \mu F$$

Charge will be same for each capacitor in series combination, so  $Q = Q_1 = Q_2 = Q_3$

$$Q = C_{eq} V$$

$$Q = (1.3 \mu F)(6 V)$$

$$Q = 7.8 \mu C$$

Voltage across 1<sup>st</sup> capacitor

$$Q = C_1 V_1$$

$$V_1 = \frac{Q}{C_1}$$

$$V_1 = \frac{7.8 \mu C}{3.0 \mu F}$$

$$V_1 = 2.6 V$$

Voltage across 2<sup>nd</sup> capacitor

$$Q = C_2 V_2$$

$$V_2 = \frac{Q}{C_2}$$

$$V_2 = \frac{7.8 \mu C}{4.0 \mu F}$$

$$V_2 = 1.95 V$$

Voltage across 3<sup>rd</sup> capacitor

$$Q = C_3 V_3$$

$$V_3 = \frac{Q}{C_3}$$

$$V_3 = \frac{7.8 \mu C}{5.0 \mu F}$$

$$V_3 = 1.56 V$$